

SM3 1.2 NH: Factoring with Three or Four Terms

Factor by Grouping: Factor each completely over the integers.

1) $7x^3 + 4x^2 + 42x + 24$
 $(x^2 + 6)(7x + 4)$

2) $21m^3 + 7m^2 - 18m - 6$
 $(7m^2 - 6)(3m + 1)$

3) $54k^3 + 144k^2 + 9k + 24$
 $3(6k^2 + 1)(3k + 8)$

4) $2k^3 + 7k^2 + 14k + 49$
 $(k^2 + 7)(2k + 7)$

5) $64n^4 - 256n^3 - 40n^2 + 160n$
 $8n(8n^2 - 5)(n - 4)$

6) $18p^5 + 12p^4 - 54p^3 - 36p^2$
 $6p^2(p^3 - 3)(3p + 2)$

7) $2x^3 + x^2 - 8x - 4$
 $(x + 2)(x - 2)(2x + 1)$

8) $x^4 + x^3 - 27x - 27$
 $(x - 3)(x^2 + 3x + 9)(x + 1)$

Three terms: Factor each completely over the integers.

9) $2b^2 + 3b - 54$
 $(b + 6)(2b - 9)$

10) $5a^2 + 7a - 6$
 $(a + 2)(5a - 3)$

11) $7x^2 - 44x + 45$
 $(x - 5)(7x - 9)$

12) $3x^2 + x - 14$
 $(3x + 7)(x - 2)$

13) $15n^2 + 69n + 72$
 $3(n + 3)(5n + 8)$

14) $-7n^2 + 57n + 54$
 $-(n - 9)(7n + 6)$

15) $-5a^2 + 46a + 40$
 $-(a - 10)(5a + 4)$

16) $10m^2 - 48m + 54$
 $2(m - 3)(5m - 9)$

17) $4x^2 + 32x + 64$
 $4(x + 4)^2$

18) $n^2 - 10n + 16$
 $(n - 2)(n - 8)$

19) $m^2 + 3m - 54$
 $(m + 9)(m - 6)$

20) $r^2 + 12r + 27$
 $(r + 9)(r + 3)$

21) $16n^2 - 140n + 96$
 $4(n - 8)(4n - 3)$

22) $-6x^2 + 17x + 10$
 $-(3x - 10)(2x + 1)$

23) $4x^2 - 9x - 9$
 $(x - 3)(4x + 3)$

24) $9p^2 - 8p - 45$
prime

25) $k^2 - 2k - 14$
prime

26) $9n^2 + 12n + 4$
 $(3n + 2)^2$

27) $25k^2 + 20k + 4$
 $(5k + 2)^2$

28) $m^2 + 5m - 20$
prime

Quadratic Form: Factor each completely over the integers.

$$29) \quad x^4 - 12x^2 + 27 \\ (x + 3)(x - 3)(x^2 - 3)$$

$$30) \quad m^6 - 4m^3 - 21 \\ (m^3 - 7)(m^3 + 3)$$

$$31) \quad 4x^6 - 12x^3 - 160 \\ 4(x - 2)(x^2 + 2x + 4)(x^3 + 5)$$

$$32) \quad x^4 + 4x^2 - 21 \\ (x^2 + 7)(x^2 - 3)$$

$$33) \quad 3a^4 + 15a^2 + 12 \\ 3(a^2 + 4)(a^2 + 1)$$

$$34) \quad 6a^4 - 12a^2 - 480 \\ 6(a^2 - 10)(a^2 + 8)$$

$$35) \quad 5x^8 - 50x^4 + 120 \\ 5(x^4 - 6)(x^2 + 2)(x^2 - 2)$$

$$36) \quad x^8 + 11x^4 + 28 \\ (x^4 + 7)(x^4 + 4)$$

$$37) \quad x^6 - x^4 - x^2 + 1 \\ (x^2 + 1)(x + 1)^2(x - 1)^2$$

$$38) \quad x^6 + x^4 - 16x^2 - 16 \\ (x^2 + 4)(x + 2)(x - 2)(x^2 + 1)$$